

Experiment 10

Ram Sundar.R

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#1. Compute the QR factorization, SVD and Least square solution For \ the given matrices. $A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 4 & 5 \\ 6 & 2 & 1 \end{bmatrix}$ $B = \begin{bmatrix} -1 & 0 & 1 \\ 2 & 1 & 5 \\ 3 & 5 & 6 \end{bmatrix}$

$A = \begin{bmatrix} 1 & 2 & 3 \\ 4 & 4 & 5 \\ 6 & 2 & 1 \end{bmatrix}$

$B = \begin{bmatrix} -1 & 0 & 1 \\ 2 & 1 & 5 \\ 3 & 5 & 6 \end{bmatrix}$

$A = \text{matrix}(\text{QQ}, [\begin{bmatrix} 1 & 2 & 3 \end{bmatrix}, \begin{bmatrix} 4 & 4 & 5 \end{bmatrix}, \begin{bmatrix} 6 & 2 & 1 \end{bmatrix}])$

$B = \text{matrix}(\text{QQ}, [\begin{bmatrix} -1 & 0 & 1 \end{bmatrix}, \begin{bmatrix} 2 & 1 & 5 \end{bmatrix}, \begin{bmatrix} 3 & 5 & 6 \end{bmatrix}])$

$V = \text{QQ}^3$

$W = \text{QQ}^3$

$U = \text{QQ}^3$

$T = \text{linear_transformation}(W, V, A)$

$S = \text{linear_transformation}(U, V, B)$

T

S

$C = T * S$

C

$\text{matrix_A} = A.\text{change_ring}(\text{QQ})$

$\text{matrix_B} = B.\text{change_ring}(\text{QQ})$

$\text{matrix_C} = C.\text{matrix}()$

$\text{matrix_AB} = \text{matrix_A} * \text{matrix_B}$

$\text{matrix_AB} == \text{matrix_C}$

Vector space morphism represented by the matrix:

$\begin{bmatrix} 1 & 2 & 3 \end{bmatrix}$

$\begin{bmatrix} 4 & 4 & 5 \end{bmatrix}$

$\begin{bmatrix} 6 & 2 & 1 \end{bmatrix}$

Domain: Vector space of dimension 3 over Rational Field

Codomain: Vector space of dimension 3 over Rational Field

Vector space morphism represented by the matrix:

$\begin{bmatrix} -1 & 0 & 1 \end{bmatrix}$

$\begin{bmatrix} 2 & 1 & 5 \end{bmatrix}$

$\begin{bmatrix} 3 & 5 & 6 \end{bmatrix}$

Domain: Vector space of dimension 3 over Rational Field

Codomain: Vector space of dimension 3 over Rational Field

Vector space morphism represented by the matrix:

$\begin{bmatrix} 5 & 0 & -2 \end{bmatrix}$

[36 18 16]

[59 38 40]

Domain: Vector space of dimension 3 over Rational Field

Codomain: Vector space of dimension 3 over Rational Field

False

#2. Compute the QR factorization, SVD and Least square solution for \ the given matrices $A = \begin{bmatrix} 1 & 1 & 1 \\ 2 & 2 & 2 \\ 3 & 1 & -1 \end{bmatrix}$ $B = \begin{bmatrix} 3 & 2 & 3 \\ 2 & 1 & 2 \\ 6 & 2 & 1 \end{bmatrix}$

$A = \begin{bmatrix} 1 & 1 & 1 \\ 2 & 2 & 2 \\ 3 & 1 & -1 \end{bmatrix}$

$B = \begin{bmatrix} 3 & 2 & 3 \\ 2 & 1 & 2 \\ 6 & 2 & 1 \end{bmatrix}$

$A = \text{matrix}(\text{QQ}, [[1, 1, 1], [2, 2, 2], [3, 1, -1]])$

$B = \text{matrix}(\text{QQ}, [[3, 2, 3], [2, 1, 2], [6, 2, 1]])$

$V = \text{QQ}^3$

$W = \text{QQ}^3$

$U = \text{QQ}^3$

$T = \text{linear_transformation}(W, V, A)$

$S = \text{linear_transformation}(U, V, B)$

T

S

$C = T * S$

C

$\text{matrix_A} = A.\text{change_ring}(\text{QQ})$

$\text{matrix_B} = B.\text{change_ring}(\text{QQ})$

$\text{matrix_C} = C.\text{matrix}()$

$\text{matrix_AB} = \text{matrix_A} * \text{matrix_B}$

$\text{matrix_AB} == \text{matrix_C}$

Vector space morphism represented by the matrix:

$\begin{bmatrix} 1 & 1 & 1 \\ 2 & 2 & 2 \\ 3 & 1 & -1 \end{bmatrix}$

$\begin{bmatrix} 2 & 2 & 2 \\ 2 & 1 & 2 \\ 6 & 2 & 1 \end{bmatrix}$

$\begin{bmatrix} 3 & 1 & -1 \end{bmatrix}$

Domain: Vector space of dimension 3 over Rational Field

Codomain: Vector space of dimension 3 over Rational Field

Vector space morphism represented by the matrix:

$\begin{bmatrix} 3 & 2 & 3 \\ 2 & 1 & 2 \\ 6 & 2 & 1 \end{bmatrix}$

$\begin{bmatrix} 2 & 1 & 2 \\ 6 & 2 & 1 \end{bmatrix}$

$\begin{bmatrix} 6 & 2 & 1 \end{bmatrix}$

Domain: Vector space of dimension 3 over Rational Field

Codomain: Vector space of dimension 3 over Rational Field

Vector space morphism represented by the matrix:

$\begin{bmatrix} 16 & 10 & 4 \\ 10 & 6 & 2 \\ 13 & 11 & 9 \end{bmatrix}$

$\begin{bmatrix} 10 & 6 & 2 \\ 13 & 11 & 9 \end{bmatrix}$

$\begin{bmatrix} 13 & 11 & 9 \end{bmatrix}$

Domain: Vector space of dimension 3 over Rational Field

Codomain: Vector space of dimension 3 over Rational Field

False